

Please write clearly in block capitals.

Centre number

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Surname

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Forename(s)

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Candidate signature

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I declare this is my own work.



# A-level MATHEMATICS

## Paper 2

Wednesday 10 June 2020

Afternoon

Time allowed: 2 hours

### Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
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<b>TOTAL</b>	



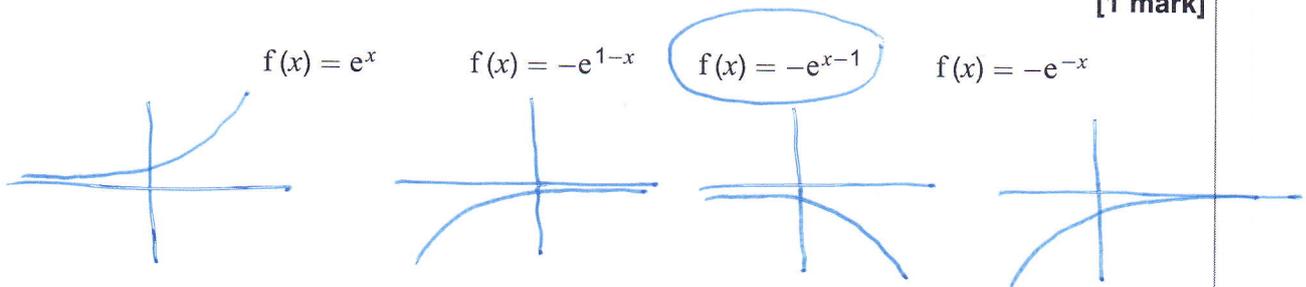
## Section A

Do not write  
outside the  
boxAnswer **all** questions in the spaces provided.

- 1 Which one of these functions is decreasing for all real values of  $x$ ?

Circle your answer.

[1 mark]



- 2 Which one of the following equations has no real solutions?

Tick (✓) **one** box.

[1 mark]

$\cot x = 0$

$\ln x = 0$

$|x + 1| = 0$

$\sec x = 0$

$\frac{1}{\sin x} = 0$



- 3 Find the coefficient of  $x^2$  in the binomial expansion of  $\left(2x - \frac{3}{x}\right)^8$

[3 marks]

$$\begin{aligned} & {}^8C_0 (2x)^8 \left(-\frac{3}{x}\right)^0 + {}^8C_1 (2x)^7 \left(-\frac{3}{x}\right)^1 \\ & + {}^8C_2 (2x)^6 \left(-\frac{3}{x}\right)^2 \\ & + {}^8C_3 (2x)^5 \left(-\frac{3}{x}\right)^3 + \dots \end{aligned}$$

Only term to produce  $x^2$  is

$${}^8C_3 (2x)^5 \left(-\frac{3}{x}\right)^3$$

$$= 56 \times 32 x^5 \times -\frac{27}{x^3}$$

$$= -48384 x^2$$

coefficient of  $x^2$  is  $-48384$

Turn over for the next question

Turn over ►



4

Using small angle approximations, show that for small, non-zero, values of  $x$

$$\frac{x \tan 5x}{\cos 4x - 1} \approx A$$

where  $A$  is a constant to be determined.

[4 marks]

small angles  $\tan \theta \approx \theta$

$$\cos \theta \approx 1 - \frac{\theta^2}{2}$$

$$\frac{x \times 5x}{1 - \frac{(4x)^2}{2}} \approx \frac{5x^2}{16x^2} \times 2$$

$$\approx \frac{10}{16} \approx \frac{5}{8}$$

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5

Use integration by substitution to show that

$$\int_{-\frac{1}{4}}^6 x\sqrt{4x+1} dx = \frac{875}{12}$$

Fully justify your answer.

[6 marks]

$$\text{let } u = 4x + 1 \Rightarrow x = \frac{u-1}{4}$$

$$\frac{du}{dx} = 4 \Rightarrow dx = \frac{du}{4}$$

$$\text{limits } x = 6, u = 25$$

$$x = -\frac{1}{4}, u = 0$$

$$\int_0^{25} \frac{u-1}{4} \times u^{\frac{1}{2}} \times \frac{du}{4}$$

$$= \frac{1}{16} \int_0^{25} u^{\frac{3}{2}} - u^{\frac{1}{2}} du$$

$$= \frac{1}{16} \left[ \frac{2}{5} u^{\frac{5}{2}} - \frac{2}{3} u^{\frac{3}{2}} \right]_0^{25}$$

$$= \frac{1}{16} \left[ \left( 1250 - \frac{250}{3} \right) - (0-0) \right]$$

$$= \frac{1}{16} \left[ \frac{3500}{3} \right] = \frac{875}{12}$$

as required

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6 The line  $L$  has equation

$$5y + 12x = 298 \quad (1)$$

A circle,  $C$ , has centre  $(7, 9)$

$L$  is a tangent to  $C$ .

6 (a) Find the coordinates of the point of intersection of  $L$  and  $C$ .

Fully justify your answer.

[5 marks]

$$L \quad 5y = -12x + 298$$

$$y = -\frac{12}{5}x + \frac{298}{5}$$

gradient of tangent is  $-\frac{12}{5}$

$\therefore$  gradient of radius from  $(7, 9)$  is  $\frac{5}{12}$  as perpendicular

$$y - y_1 = m(x - x_1)$$

$$y - 9 = \frac{5}{12}(x - 7)$$

$$12(y - 9) = 5(x - 7)$$

$$12y - 108 = 5x - 35$$

$$-73 = 5x - 12y \quad (2)$$

Solve (1) and (2) simultaneously

$$5y + 12x = 298 \quad (1) \times 12$$

$$-12y + 5x = -73 \quad (2) \times 5$$

$$60y + 144x = 3576 \quad (1)$$

$$-60y + 25x = -365 \quad (2)$$

$$(1) + (2) \quad 169x = 3211$$

$$x = 19$$

$$\text{in (1)} \quad y = \frac{298 - 12 \times 19}{5} = 14$$

$L$  and  $C$  intersect at  $(19, 14)$



6 (b) Find the equation of C.

[3 marks]

Length  $LC = \sqrt{(19-7)^2 + (14-9)^2}$

$LC = 13$  (radius)

Equation of C

$(x-7)^2 + (y-9)^2 = 169$

Turn over for the next question

Turn over ►



7  $a$  and  $b$  are two positive irrational numbers.

The sum of  $a$  and  $b$  is rational.

The product of  $a$  and  $b$  is rational.

Caroline is trying to prove  $\frac{1}{a} + \frac{1}{b}$  is rational.

Here is her proof:

Step 1  $\frac{1}{a} + \frac{1}{b} = \frac{2}{a+b}$

Step 2 2 is rational and  $a+b$  is non-zero and rational.

Step 3 Therefore  $\frac{2}{a+b}$  is rational.

Step 4 Hence  $\frac{1}{a} + \frac{1}{b}$  is rational.

7 (a) (i) Identify Caroline's mistake.

[1 mark]

Step 1  $\frac{1}{a} + \frac{1}{b} = \frac{b+a}{ab}$   
not  $\frac{2}{a+b}$

7 (a) (ii) Write down a correct version of the proof.

[2 marks]

$$\frac{1}{a} + \frac{1}{b} = \frac{b+a}{ab}$$

Numerator (sum of  $a$  and  $b$ ) is rational  
Denominator  $ab$  is rational and non zero

$\therefore$  rational divided by a rational  
gives a rational

$\therefore \frac{1}{a} + \frac{1}{b}$  is rational



- 7 (b) Prove by contradiction that the difference of any rational number and any irrational number is irrational.

[4 marks]

Assume that the difference  
between a rational number  $\frac{a}{b}$   
and an irrational number  $\frac{c}{d}$   
is rational  $x$ , where  $a, b, c, d$   
are integers and

$$\therefore \frac{a}{b} - x = \frac{c}{d} \quad b \text{ and } d \neq 0$$

$\uparrow$                      $\uparrow$                      $\uparrow$   
 rational          rational          irrational

rearranging

$$\frac{a}{b} - \frac{c}{d} = x$$

$$\frac{ad - bc}{bd} = x$$

$ad - bc$  is an integer

$bd$  is an integer

$\therefore \frac{ad - bc}{bd}$  is rational

$\therefore x$  is rational. As this  
contradicts our original  
assumption, then the  
difference between a rational  
number and irrational  
number is irrational

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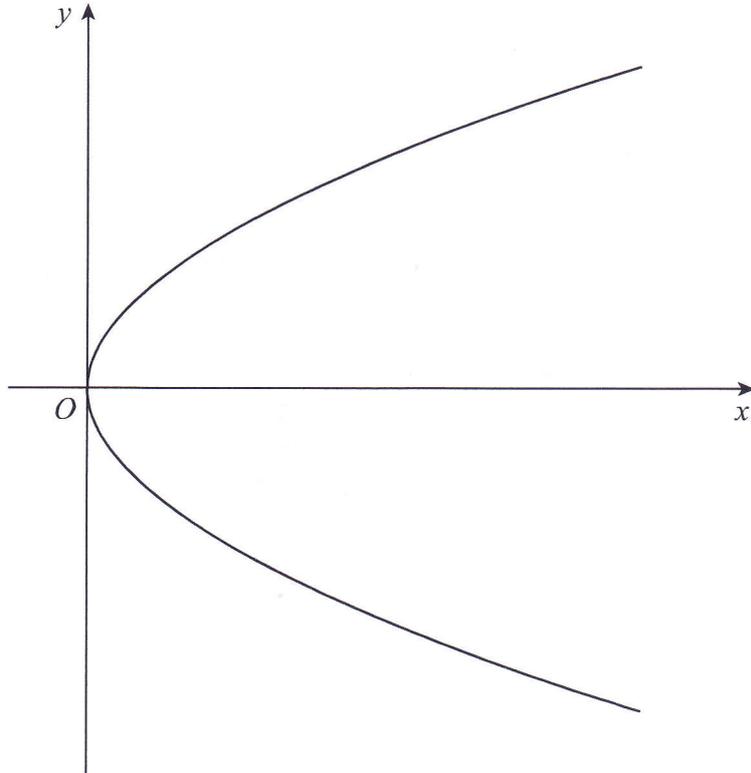


- 8 The curve defined by the parametric equations

$$x = t^2 \text{ and } y = 2t \quad -\sqrt{2} \leq t \leq \sqrt{2}$$

is shown in **Figure 1** below.

**Figure 1**



- 8 (a) Find a Cartesian equation of the curve in the form  $y^2 = f(x)$

[2 marks]

$$x = t^2 \qquad y = 2t$$

$$\sqrt{x} = t$$

$$y = 2\sqrt{x}$$

$$y^2 = 4x$$

Turn over ►

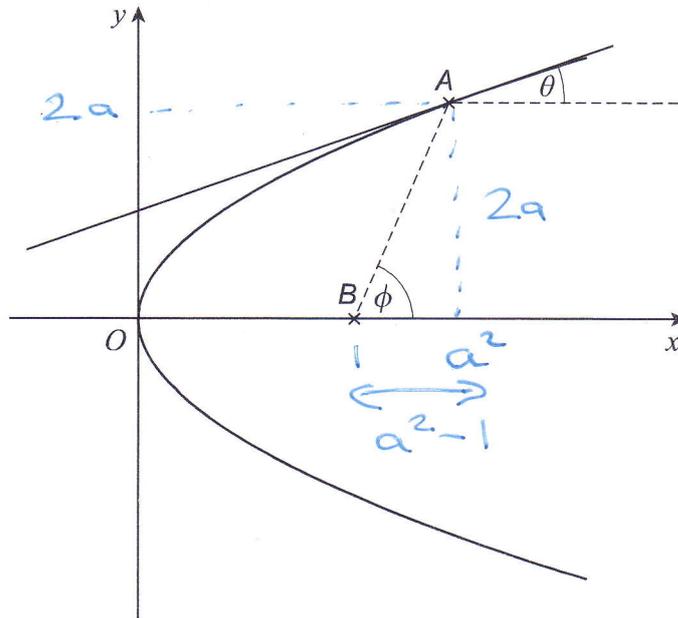


8 (b) The point  $A$  lies on the curve where  $t = a$

The tangent to the curve at  $A$  is at an angle  $\theta$  to a line through  $A$  parallel to the  $x$ -axis.

The point  $B$  has coordinates  $(1, 0)$

The line  $AB$  is at an angle  $\phi$  to the  $x$ -axis.



8 (b) (i) By considering the gradient of the curve, show that

$$\tan \theta = \frac{1}{a}$$

[3 marks]

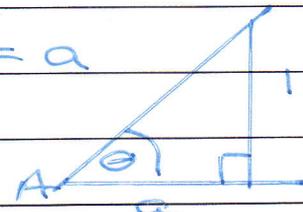
$$x = t^2 \quad y = 2t$$

$$\frac{dx}{dt} = 2t \quad \frac{dy}{dt} = 2$$

$$\frac{dy}{dx} = \frac{2}{2t} = \frac{1}{t}$$

gradient at  $t = a$

$$\frac{dy}{dx} = \frac{1}{a}$$



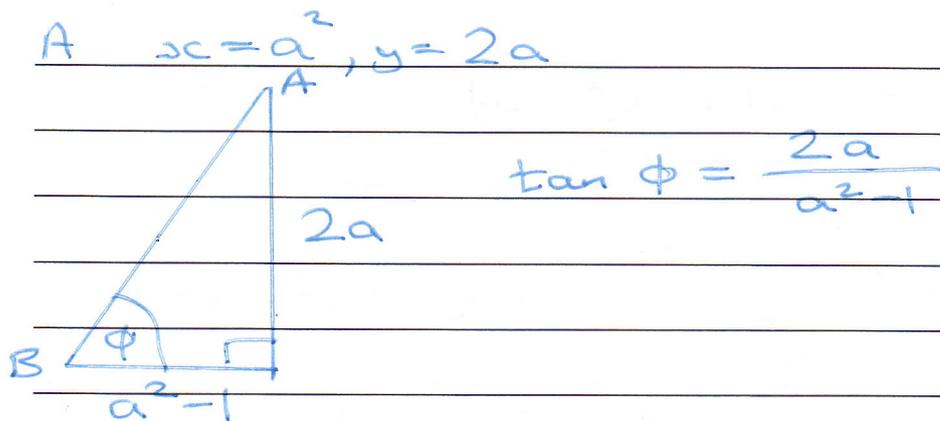
From diagram  $\tan \theta$  is the gradient

$$\text{at } a, \frac{\text{change in } y}{\text{change in } x} \therefore \tan \theta = \frac{1}{a}$$



8 (b) (ii) Find  $\tan \phi$  in terms of  $a$ .

[2 marks]



8 (b) (iii) Show that  $\tan 2\theta = \tan \phi$

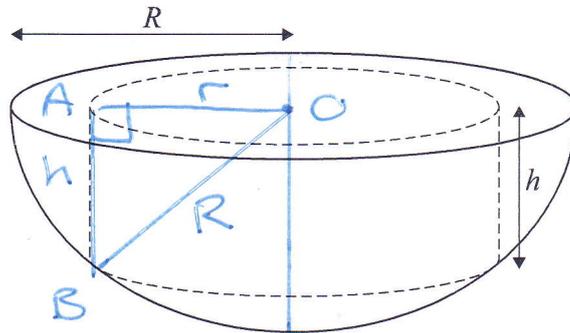
[3 marks]

$$\begin{aligned} \tan 2\theta &= \frac{\tan \theta + \tan \theta}{1 - \tan \theta \tan \theta} \\ &= \frac{\frac{1}{a} + \frac{1}{a}}{1 - \frac{1}{a} \times \frac{1}{a}} \\ &= \frac{\frac{2}{a}}{\frac{a^2 - 1}{a^2}} = \frac{2}{a} \times \frac{a^2}{a^2 - 1} \\ &= \frac{2a}{a^2 - 1} \\ &= \tan \phi \end{aligned}$$

Turn over ►



- 9 A cylinder is to be cut out of the circular face of a solid hemisphere. The cylinder and the hemisphere have the same axis of symmetry. The cylinder has height  $h$  and the hemisphere has a radius of  $R$ .



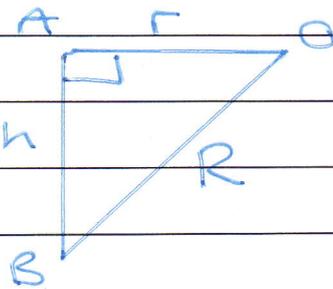
- 9 (a) Show that the volume,  $V$ , of the cylinder is given by

$$V = \pi R^2 h - \pi h^3$$

[3 marks]

let radius of cylinder =  $r$

$$V = \pi r^2 h \quad (1)$$



Using Pythagoras

$$r^2 = R^2 - h^2$$

substitute in (1)

$$V = \pi (R^2 - h^2) h$$

$$V = \pi R^2 h - \pi h^3$$

as required



9 (b) Find the maximum volume of the cylinder in terms of  $R$ .

Fully justify your answer.

[7 marks]

$$V = \pi R^2 h - \pi h^3 \quad (1)$$

$$\frac{dV}{dh} = \pi R^2 - 3\pi h^2$$

max volume when  $\frac{dV}{dh} = 0$

$$0 = \pi(R^2 - 3h^2)$$

$$\therefore R^2 = 3h^2 \quad (2)$$

$$\frac{R^2}{3} = h^2 \Rightarrow h = \frac{R}{\sqrt{3}}$$

in (1)  $V = \pi \times R^2 \times \frac{R}{\sqrt{3}} - \pi \times \frac{R^3}{3\sqrt{3}}$

$$V = \pi R^3 \left( \frac{1}{\sqrt{3}} - \frac{1}{3\sqrt{3}} \right)$$

$$V = \pi R^3 \left( \frac{3-1}{3\sqrt{3}} \right)$$

$$V = \pi R^3 \times \frac{2}{3\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \pi R^3 \times \frac{2\sqrt{3}}{9}$$

$$V = \frac{2\sqrt{3}}{9} \pi R^3$$

$$\frac{d^2V}{dh^2} = -6\pi h$$

when  $h = \frac{R}{\sqrt{3}}$

$$\frac{d^2V}{dh^2} = -6\pi \times \frac{R}{\sqrt{3}} < 0$$

$\therefore$  maximum volume

Turn over for Section B

Turn over ►



## Section B

Answer **all** questions in the spaces provided.

- 10 A vehicle is driven at a constant speed of  $12 \text{ m s}^{-1}$  along a straight horizontal road.  
Only one of the statements below is correct.  
Identify the correct statement.

Tick (✓) **one** box.

[1 mark]

The vehicle is accelerating

The vehicle's driving force exceeds the total force resisting its motion

The resultant force acting on the vehicle is zero

The resultant force acting on the vehicle is dependent on its mass

- 11 A number of forces act on a particle such that the resultant force is  $\begin{pmatrix} 6 \\ -3 \end{pmatrix} \text{ N}$

One of the forces acting on the particle is  $\begin{pmatrix} 8 \\ -5 \end{pmatrix} \text{ N}$

Calculate the total of the other forces acting on the particle.

Circle your answer.

[1 mark]

$$\begin{pmatrix} 2 \\ -2 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} 14 \\ -8 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} -2 \\ 2 \end{pmatrix} \text{ N}$$

$$\begin{pmatrix} -14 \\ 8 \end{pmatrix} \text{ N}$$



12

A particle,  $P$ , is moving with constant velocity  $8\mathbf{i} - 12\mathbf{j}$

A second particle,  $Q$ , is moving with constant velocity  $a\mathbf{i} + 9\mathbf{j}$

$Q$  travels in a direction which is parallel to the motion of  $P$ .

Find  $a$ .

Circle your answer.

$$8x - \frac{9}{12} = -6$$

[1 mark]

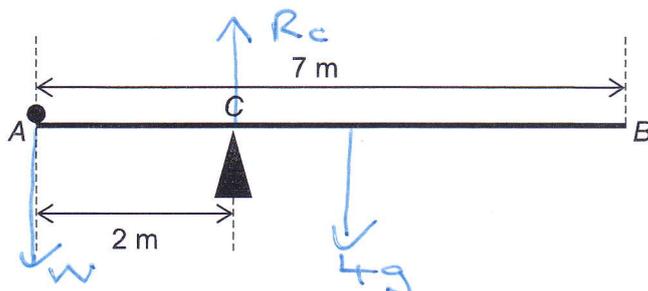
 -6 -5 5 6

Turn over for the next question

Turn over ►



- 13 A uniform rod,  $AB$ , has length 7 metres and mass 4 kilograms.
- The rod rests on a single fixed pivot point,  $C$ , where  $AC = 2$  metres.
- A particle of weight  $W$  newtons is fixed at  $A$ , as shown in the diagram.



The system is in equilibrium with the rod resting horizontally.

- 13 (a) Find  $W$ , giving your answer in terms of  $g$ .

[2 marks]

$$m(c) \quad 2W = 1.5 \times 4g$$

$$W = \frac{1.5 \times 4}{2} g$$

$$W = 3g$$

- 13 (b) Explain how you have used the fact that the rod is uniform in part (a).

[1 mark]

The rod is uniform so the centre of mass is at its midpoint



- 14 At time  $t$  seconds a particle,  $P$ , has position vector  $\mathbf{r}$  metres, with respect to a fixed origin, such that

$$\mathbf{r} = (t^3 - 5t^2)\mathbf{i} + (8t - t^2)\mathbf{j}$$

- 14 (a) Find the exact speed of  $P$  when  $t = 2$

[4 marks]

$$\underline{r} = \begin{pmatrix} t^3 - 5t^2 \\ 8t - t^2 \end{pmatrix}$$

differentiating

$$\underline{v} = \begin{pmatrix} 3t^2 - 10t \\ 8 - 2t \end{pmatrix}$$

$$\text{at } t=2, \underline{v} = \begin{pmatrix} 3 \times 2^2 - 10 \times 2 \\ 8 - 2 \times 2 \end{pmatrix}$$

$$\underline{v} = \begin{pmatrix} -8 \\ 4 \end{pmatrix}$$

$$\text{speed} = \sqrt{(-8)^2 + (4)^2} = 4\sqrt{5} \text{ m s}^{-1}$$

- 14 (b) Bella claims that the magnitude of acceleration of  $P$  will never be zero.

Determine whether Bella's claim is correct.

Fully justify your answer.

[3 marks]

$$\underline{v} = \begin{pmatrix} 3t^2 - 10t \\ 8 - 2t \end{pmatrix}$$

differentiating

$$\underline{a} = \begin{pmatrix} 6t - 10 \\ -2 \end{pmatrix}$$

$$|\underline{a}| = \sqrt{(6t - 10)^2 + (-2)^2}$$

smallest that  $(6t - 10)^2$  can be is zero

so  $|\underline{a}| \geq 2$

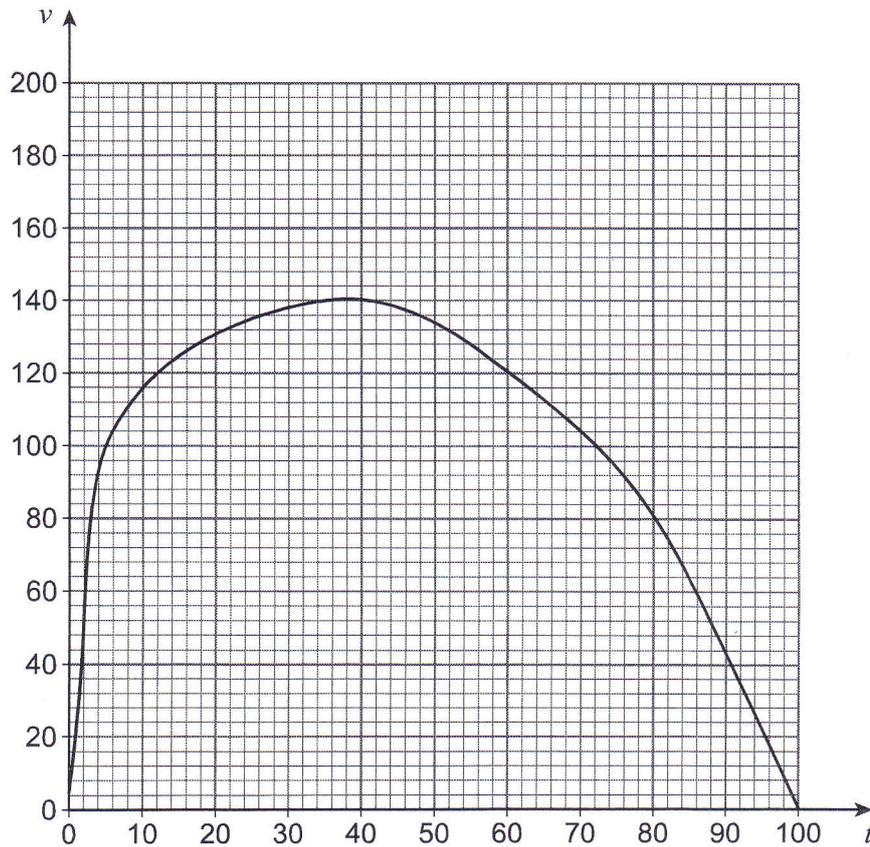
Bella is correct, the magnitude of the acceleration will never be zero

Turn over ▶



15

A particle is moving in a straight line with velocity  $v \text{ m s}^{-1}$  at time  $t$  seconds as shown by the graph below.



15 (a)

Use the trapezium rule with four strips to estimate the distance travelled by the particle during the time period  $20 \leq t \leq 100$

[4 marks]

$t$	20	40	60	80	100
$v$	130	140	120	80	0

$$\begin{aligned} \text{distance} &= \frac{1}{2} \times 20 (130 + 0 + \\ &\quad 2(140 + 120 + 80)) \\ &= 8100 \end{aligned}$$



- 15 (b) Over the same time period, the curve can be very closely modelled by a particular quadratic.

Explain how you could find an alternative estimate using this quadratic.

[1 mark]

Integrate to find the area  
under the quadratic between  
limits 20 and 100

Turn over for the next question

Turn over ►



16

Two particles A and B are released from rest from different starting points above a horizontal surface.

A is released from a height of  $h$  metres.

B is released at a time  $t$  seconds after A from a height of  $kh$  metres, where  $0 < k < 1$

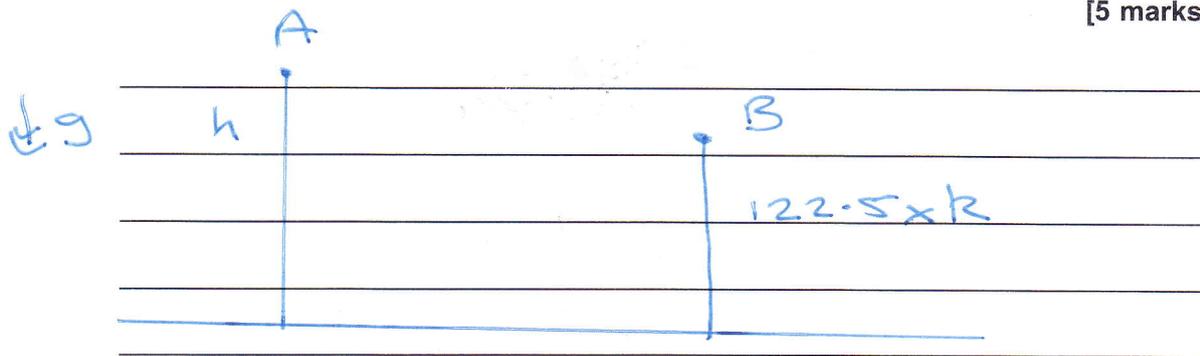
Both particles land on the surface 5 seconds after A was released.

Assuming any resistance forces may be ignored, prove that

$$t = 5(1 - \sqrt{k})$$

Fully justify your answer.

[5 marks]



for A find height  $h$

+ve ↓

$$s = h$$

$$u = 0 \text{ m s}^{-1}$$

$$v = ?$$

$$a = g$$

$$t = 5 \text{ s}$$

$$s = ut + \frac{1}{2}at^2$$

$$s = 0 + \frac{1}{2} \times 9.8 \times 25$$

$$s = 122.5 \text{ m}$$

for B  $s = 122.5 \times k$  m

$$u = 0 \text{ m s}^{-1}$$

$$v =$$

$$a = g \text{ m s}^{-2}$$

$$t = (5 - t) \text{ s}$$

$$s = ut + \frac{1}{2}at^2$$

$$122.5k = 0 + \frac{1}{2} \times 9.8 \times (5-t)^2$$

$$\frac{122.5k}{4.9} = (5-t)^2$$

$$25k = (5-t)^2$$

square root both sides



$$S\sqrt{r} = S - t$$

$$t = S - S\sqrt{r}$$

$$t = S(1 - \sqrt{r})$$

Turn over for the next question

Turn over ►



17

A ball is projected forward from a fixed point,  $P$ , on a horizontal surface with an initial speed  $u \text{ m s}^{-1}$ , at an acute angle  $\theta$  above the horizontal.

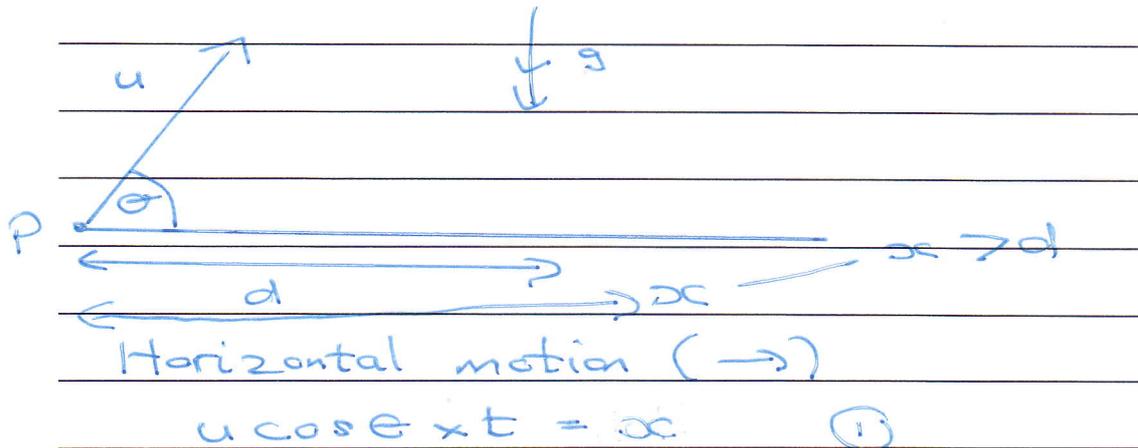
The ball needs to first land at a point at least  $d$  metres away from  $P$ .

You may assume the ball may be modelled as a particle and that air resistance may be ignored.

Show that

$$\sin 2\theta \geq \frac{dg}{u^2}$$

[6 marks]



Vertical motion ( $\uparrow$ ) +ve

$$s = 0$$

$$u = u \sin \theta \text{ m s}^{-1}$$

$$v =$$

$$a = -g \text{ m s}^{-2}$$

$$t = t$$

$$s = ut + \frac{1}{2} at^2$$

$$0 = u \sin \theta \times t - \frac{1}{2} \times g \times t^2$$

$$0 = t \left( u \sin \theta - \frac{1}{2} g t \right)$$

$$\text{Either } t = 0 \text{ or } \frac{1}{2} g t = u \sin \theta$$

$$t = \frac{2u \sin \theta}{g}$$



sub t in (1)

$$x = u \cos \theta \times \frac{2u \sin \theta}{g}$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$x = \frac{u^2 \times \sin 2\theta}{g}$$

now  $x \geq d$

$$\therefore \frac{u^2 \sin 2\theta}{g} \geq d$$

$$\sin 2\theta \geq \frac{dg}{u^2}$$

as required

Turn over for the next question

Turn over ►

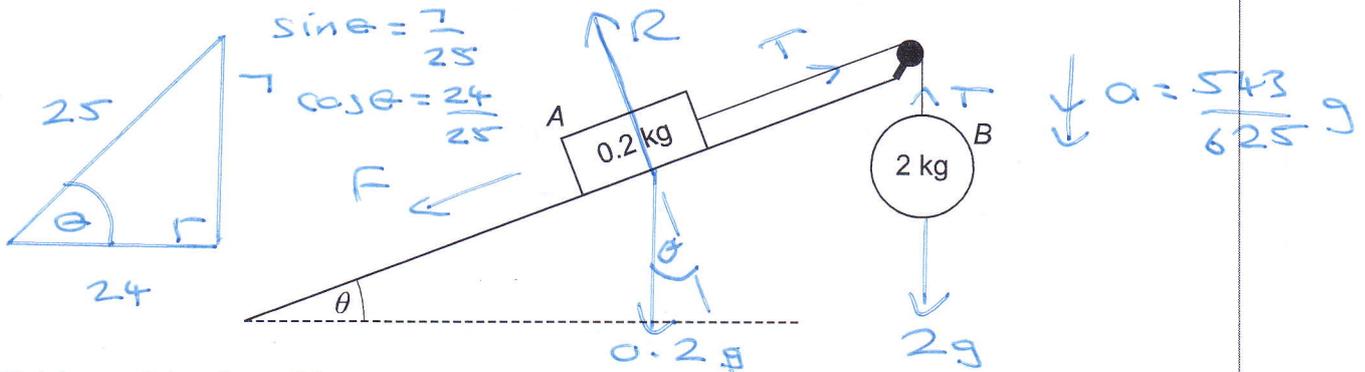


18 Block A, of mass 0.2 kg, lies at rest on a rough plane.

The plane is inclined at an angle  $\theta$  to the horizontal, such that  $\tan \theta = \frac{7}{24}$

A light inextensible string is attached to A and runs parallel to the line of greatest slope until it passes over a smooth fixed pulley at the top of the slope.

The other end of this string is attached to particle B, of mass 2 kg, which is held at rest so that the string is taut, as shown in the diagram below.



18 (a) B is released from rest so that it begins to move vertically downwards with an acceleration of  $\frac{543}{625} \text{ gms}^{-2}$

Show that the coefficient of friction between A and the surface of the inclined plane is 0.17

[8 marks]

$R (\downarrow)$  for B

$$2g - T = 2 \times \frac{543}{625} g$$

$$T = 2 \times 9.8 - \frac{2 \times 543}{625} \times 9.8 = 2.57152 \text{ N}$$

$R (\rightarrow)$  parallel to plane for A

$$0.2 \times \frac{543}{625} g = T - F - 0.2g \sin \theta$$

$$F = 2.57152 - 0.2 \times 9.8 \times \frac{7}{25} - 0.2 \times \frac{543}{625} \times 9.8$$

$$F = 0.319872 \text{ N}$$



$R(\uparrow)$  perpendicular to plane for A

$$0 = R - 0.2g \cos \theta$$

$$R = 0.2 \times 9.8 \times \frac{24}{25}$$

$$R = 1.8816 \text{ N}$$

Limiting friction

$$F = \mu R$$

$$\mu = \frac{F}{R} = \frac{0.319872}{1.8816}$$

$$\mu = 0.17$$

as required

Turn over ►



18 (b) In this question use  $g = 9.81 \text{ m s}^{-2}$

When A reaches a speed of  $0.5 \text{ m s}^{-1}$  the string breaks.  $T=0$

18 (b) (i) Find the distance travelled by A after the string breaks until first coming to rest.

[4 marks]

$$R(\text{N}) \quad R = 0.2 \times 9.81 \times \frac{24}{25}$$

$$R = 1.88352 \text{ N}$$

$$F = \mu R = 0.17 \times 1.88352$$

$$= 0.3201984 \text{ N}$$

new equation of motion for A

$$0.2 \times a = -F - 0.2g \sin \theta$$

$$a = \frac{-0.3201984 - 0.2 \times 9.81 \times \frac{7}{25}}{0.2}$$

$$a = -4.347792 \text{ m s}^{-2}$$

$$s = ?$$

$$u = 0.5 \text{ m s}^{-1}$$

$$v = 0 \text{ m s}^{-1}$$

$$a = -4.347792 \text{ m s}^{-2}$$

t

$$v^2 = u^2 + 2as$$

$$s = \frac{v^2 - u^2}{2a} = \frac{0^2 - 0.5^2}{2 \times -4.347792}$$

$$s = 0.028750 \text{ m}$$

$$s = 0.0288 \text{ m} \quad (3 \text{ sf})$$

18 (b) (ii) State an assumption that could affect the validity of your answer to part (b)(i).

[1 mark]

No air resistance

or

String does not obstruct block



**Turn over for the next question**

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- 19 A particle moves so that its acceleration,  $a \text{ m s}^{-2}$ , at time  $t$  seconds may be modelled in terms of its velocity,  $v \text{ m s}^{-1}$ , as

$$a = -0.1v^2$$

$$a = \frac{dv}{dt}$$

The initial velocity of the particle is  $4 \text{ m s}^{-1}$

- 19 (a) By first forming a suitable differential equation, show that

$$v = \frac{20}{5+2t}$$

[6 marks]

$$\frac{dv}{dt} = -0.1v^2$$

$$\int \frac{1}{v^2} dv = \int -0.1 dt$$

$$\int v^{-2} dv = \int -0.1 dt$$

$$-v^{-1} = -0.1t + c$$

$$-\frac{1}{v} = -0.1t + c$$

$$\text{at } t=0 \quad v=4$$

$$-\frac{1}{4} = 0 + c$$

$$c = -\frac{1}{4}$$

$$-\frac{1}{v} = -\frac{1}{10}t - \frac{1}{4}$$

$$\frac{1}{10}t + \frac{1}{4} = \frac{1}{v}$$

$$\frac{2t+5}{20} = \frac{1}{v}$$

$$v = \frac{20}{2t+5} \quad \text{as required}$$



19 (b) Find the acceleration of the particle when  $t = 5.5$

[2 marks]

when  $t = 5.5$

$$v = \frac{20}{2 \times 5.5 + 5} = 1.25 \text{ m s}^{-1}$$

$$a = -0.1 \times 1.25^2$$

$$a = -0.15625 \text{ m s}^{-2}$$

END OF QUESTIONS

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