

Please write clearly, in block capitals.

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# A-level MATHEMATICS

## Paper 2

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Practice paper – Set 1

Time allowed: 2 hours

### Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

### Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

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**Section A**

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Answer **all** questions in the spaces provided.

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**1**  $y = \sqrt[3]{x}$

Find  $\frac{dy}{dx}$

Circle your answer.

[1 mark]

$$\frac{1}{3x^{\frac{2}{3}}}$$

$$\frac{\frac{2}{3}}{x^3}$$

$$3\sqrt[2]{x}$$

$$\frac{3}{x^{\frac{2}{3}}}$$

**2** Find the number of terms in the series  $\sum_{r=n}^{2n} r^3$ , where  $n$  is a positive integer.

Circle your answer.

[1 mark]

$$n-1$$

$$n$$

$$n+1$$

$$2n$$



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**4 (a)** Show that the equation  $e^x - 3x = 0$  has a root,  $\alpha$ , that lies between 1 and 2.

**[2 marks]**

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**4 (b)** Use the Newton-Raphson method with  $x_1 = 2$  to find:

**4 (b) (i)**  $x_2$  and  $x_3$  correct to 3 decimal places.

**[2 marks]**

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4 (b) (ii)  $\alpha$  correct to 3 decimal places.

[1 mark]

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4 (c) Dan uses the Newton-Raphson method with  $x_1 = 1$  to try to find  $\alpha$ .  
Describe what happens.

[2 marks]

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**Turn over for the next question**

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6 (a) Write  $\sqrt{3}\cos\theta - 2\sin\theta$  in the form  $R\cos(\theta + \alpha)$ , where  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$

[3 marks]

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- 6 (b) A particle moves in a straight line so that its displacement,  $x$  metres from the origin, at time,  $t$  seconds, is given by

$$x = 8 \cos\left(t + \frac{\pi}{6}\right) - 2\sqrt{3} \cos t, \quad t \geq 0$$

- 6 (b) (i) Show that  $x = 2\sqrt{3} \cos t - 4 \sin t$

[3 marks]

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- 6 (b) (ii) Find the maximum displacement of the particle from the origin.

[1 mark]

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- 6 (b) (iii) State the earliest time at which the maximum displacement occurs.

[1 mark]

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**END OF SECTION A  
TURN OVER FOR SECTION B**

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**Section B**

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Answer **all** questions in the spaces provided.

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- 9** Given vectors  $\mathbf{p} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$  and  $\mathbf{q} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$ , find the value of  $|\mathbf{p} - \mathbf{q}|$

Circle your answer.

[1 mark]

1

$\sqrt{13}$

$\sqrt{5}$

5

- 10** The velocity,  $v$ , of a particle moving in a straight line is given by  $v = \cos(3t)$  at time  $t$ .

State the acceleration of the particle at time  $t$ .

Circle your answer.

[1 mark]

$3\sin(3t)$

$-3\sin(3t)$

$-\frac{1}{3}\sin(3t)$

$\sin(3t)$

- 11 Two forces  $\mathbf{F}_1$  newtons and  $\mathbf{F}_2$  newtons act on a particle:

$$\mathbf{F}_1 = (3\mathbf{i} - 2\mathbf{j})$$

$$\mathbf{F}_2 = (2\mathbf{i} + 4\mathbf{j})$$

The unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are horizontal and vertical respectively.

The resultant of these two forces is  $\mathbf{F}$  newtons.

- 11 (a) (i) Find  $\mathbf{F}$ .

[1 mark]

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- 11 (a) (ii) Find the acute angle that  $\mathbf{F}$  makes with the horizontal, giving your answer to the nearest  $0.1^\circ$ .

[2 marks]

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- 11 (b)** A third force,  $\mathbf{F}_3$  newtons, is applied to the particle.  
The resultant of the three forces is  $(-\mathbf{i} + 3\mathbf{j})$  N.

Find  $\mathbf{F}_3$ .

[1 mark]

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**Turn over for the next question**

- 12 A uniform rod,  $AB$ , has length 4 metres and mass 6 kg.  
It rests on two supports at  $C$  and  $D$ , where  $AC = 1$  metre and  $AD = 2.5$  metres.



- 12 (a) A particle of mass  $m$  kg is placed on the rod at a point  $E$ , 3.1 metres from  $A$ .

Given that the rod is on the point of tilting about  $D$ , calculate the value of  $m$ .

**[3 marks]**

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- 13 A particle moves such that its velocity,  $\mathbf{v}$  m s<sup>-1</sup>, at time  $t$  seconds is given by

$$\mathbf{v} = \begin{pmatrix} 1 - 2t^2 \\ 2t \end{pmatrix}$$

When  $t = 1$ , the displacement of the particle from a fixed origin  $O$  is  $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$  metres.

Find the displacement from  $O$  when  $t = 2$ .

**[5 marks]**

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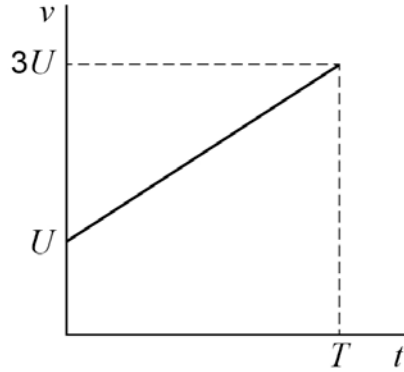
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- 14** A particle is initially at point  $O$ . It moves in a straight line with a constant acceleration of  $0.68 \text{ m s}^{-2}$ .
- The initial velocity of the particle is  $U$  metres per second.
- After  $T$  seconds, the particle has velocity  $3U$  metres per second.
- The velocity-time graph represents the motion of the particle.



- 14 (a)** The particle travels  $17 \text{ m}$  in  $T$  seconds.

Find  $U$  and  $T$ .

**[5 marks]**

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**14 (b)** Sketch a displacement-time graph for the motion of the particle.

**[1 mark]**

**Turn over for the next question**





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**15 (b)** Describe the effect of the assumption that the string is inextensible.

**[1 mark]**

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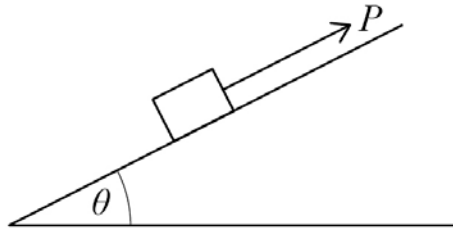
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- 16** The diagram shows a box of mass 2 kg on a rough plane inclined at  $\theta^\circ$  to the horizontal, where  $\sin \theta = \frac{3}{5}$

The coefficient of friction between the box and the plane is  $\frac{1}{3}$

The box is held in equilibrium by a force of magnitude  $P$  newtons acting up the plane as shown in the diagram.



- 16 (a)** Given that the force is just sufficient to prevent the particle from sliding down the plane, show that  $P = \frac{2g}{3}$

**[5 marks]**

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**16 (b)** The force is now removed and the box slides down the plane.

Find the speed of the box when it has travelled one sixth of a metre down the plane, giving your answer in terms of  $g$ .

**[4 marks]**

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**Turn over for the next question**

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17 Three points have position vectors  $\vec{OA} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ ,  $\vec{OB} = \begin{pmatrix} 5 \\ \sqrt{3} \\ 7 \end{pmatrix}$  and  $\vec{OC} = \begin{pmatrix} 9 + 4\sqrt{3} \\ 1 \\ 11 + 4\sqrt{3} \end{pmatrix}$

Prove that the points  $A$ ,  $B$  and  $C$  are collinear.

[4 marks]

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**Turn over for the next question**

**18** In this question use  $g = 9.81 \text{ m s}^{-2}$ .

A golfer strikes a ball from a point,  $A$ , on the ground with speed  $28.5 \text{ m s}^{-1}$  at an angle of elevation  $30^\circ$ .

The ball travels towards a tree of height  $9.5 \text{ m}$ , which is at a horizontal distance of  $45.4 \text{ m}$  from  $A$ . The base of the tree is at the same horizontal level as  $A$ .

- 18 (a)** Determine whether the ball will go over the tree.  
Fully justify your answer.

**[6 marks]**

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**18 (b)** Explain why your answer to part (a) might not be correct.

[1 mark]

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**END OF QUESTIONS**

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