Jan



5. (a) Find $\int \frac{9x+6}{x} dx$, x > 0.

(2)

(b) Given that y = 8 at x = 1, solve the differential equation

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{(9x+6)y^{\frac{1}{3}}}{x}$$

giving your answer in the form $y^2 = g(x)$.

(6)

3. (a) Express $\frac{5}{(x-1)(3x+2)}$ in partial fractions.

Janzon

(3)

(b) Hence find $\int \frac{5}{(x-1)(3x+2)} dx$, where x > 1.

(3)

(c) Find the particular solution of the differential equation

$$(x-1)(3x+2) \frac{dy}{dx} = 5y, \quad x > 1,$$

for which y = 8 at x = 2. Give your answer in the form y = f(x).

(6)

7. (a) Express $\frac{2}{4-y^2}$ in partial fractions.

June

(b) Hence obtain the solution of

$$2 \cot x \, \frac{\mathrm{d}y}{\mathrm{d}x} = (4 - y^2)$$

for which y = 0 at $x = \frac{\pi}{3}$, giving your answer in the form $\sec^2 x = g(y)$.

(8)

4. Given that y = 2 at $x = \frac{\pi}{4}$, solve the differential equation

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{3}{y\cos^2 x}$$

(5)

| | | | materia e a minimi di materiali di | monuments—un—market — mark |
|--|--|---|------------------------------------|----------------------------|
| | | | | |
| | | | | |
| | | | | |
| | | * | 44 | |
| | | | | |
| | | | | |