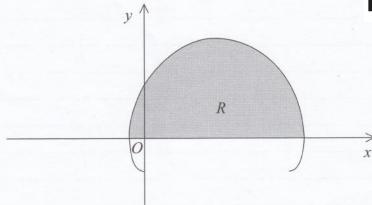
Figure 2





The curve shown in Figure 2 has parametric equations

$$x = t - 2\sin t$$
, $y = 1 - 2\cos t$, $0 \leqslant t \leqslant 2\pi$.

(a) Show that the curve crosses the x-axis where $t = \frac{\pi}{3}$ and $t = \frac{5\pi}{3}$.

(2)

The finite region R is enclosed by the curve and the x-axis, as shown shaded in Figure 2.

(b) Show that the area of R is given by the integral



$$\int_{\frac{\pi}{3}}^{\frac{5\pi}{3}} (1 - 2\cos t)^2 \mathrm{d}t.$$

(3)

(c) Use this integral to find the exact value of the shaded area.

(7)

A curve has parametric equations	
$x = 7 \cos t - \cos 7t$, $y = 7 \sin t - \sin 7t$, $\frac{\pi}{8} < t < \frac{\pi}{3}$.	
(a) Find an expression for $\frac{dy}{dx}$ in terms of t. You need not simplify your ar	iswer.
4	(3)
(b) Find an equation of the normal to the curve at the point where $t = \frac{\pi}{6}$.	
Give your answer in its simplest exact form.	
	(6)

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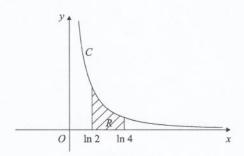


Figure 3

The curve C has parametric equations

$$x = \ln{(t+2)}, \quad y = \frac{1}{(t+1)}, \quad t > -1.$$

The finite region R between the curve C and the x-axis, bounded by the lines with equations $x = \ln 2$ and $x = \ln 4$, is shown shaded in Figure 3.

(a) Show that the area of R is given by the integral

$$\int_0^2 \frac{1}{(t+1)(t+2)} \, \mathrm{d}t.$$

(b) Hence find an exact value for this area.

(6)

(4)

Leave blank

(c) Find a cartesian equation of the curve C, in the form y = f(x).

(4)

(d) State the domain of values for x for this curve.

(1)

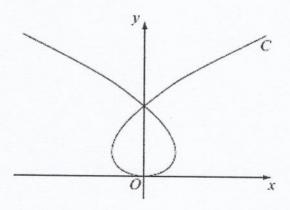


Figure 3

The curve C shown in Figure 3 has parametric equations

$$x = t^3 - 8t, \quad y = t^2$$

where t is a parameter. Given that the point A has parameter t = -1,

(a) find the coordinates of A.

(1)

The line l is the tangent to C at A.

(b) Show that an equation for l is 2x - 5y - 9 = 0.

(5)

The line l also intersects the curve at the point B.

(c) Find the coordinates of B.

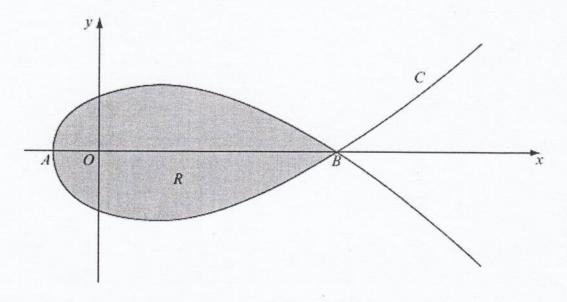


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = 5t^2 - 4$$
, $y = t(9 - t^2)$

The curve C cuts the x-axis at the points A and B.

(a) Find the x-coordinate at the point A and the x-coordinate at the point B.

(3)

The region R, as shown shaded in Figure 2, is enclosed by the loop of the curve.

(b) Use integration to find the area of R.

6. The curve C has parametric equations

$$x = \ln t$$
, $y = t^2 - 2$, $t > 0$.

Find

(a) an equation of the normal to C at the point where t = 3,

(6)

(b) a cartesian equation of C.

(3)

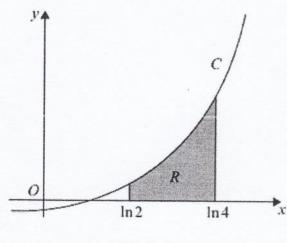


Figure 1

The finite area R, shown in Figure 1, is bounded by C, the x-axis, the line $x = \ln 2$ and the line $x = \ln 4$. The area R is rotated through 360° about the x-axis.

(c) Use calculus to find the exact volume of the solid generated.

5.

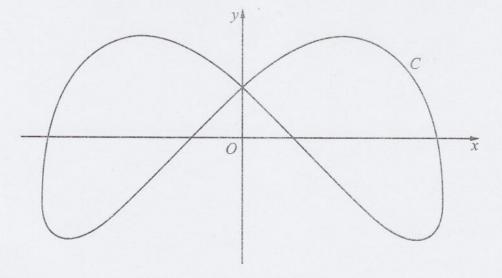


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = 4\sin\left(t + \frac{\pi}{6}\right), \quad y = 3\cos 2t, \quad 0 \leqslant t < 2\pi$$

(a) Find an expression for $\frac{dy}{dx}$ in terms of t.

(3)

(b) Find the coordinates of all the points on C where $\frac{dy}{dx} = 0$

(5)

6.	A curve has parametric equations	
	$x = 2 \cot t$, $y = 2 \sin^2 t$, $0 < t \le \frac{\pi}{2}$	

(a) Find an expression for $\frac{dy}{dx}$ in terms of the parameter t.

(4)

(b) Find an equation of the tangent to the curve at the point where $t = \frac{\pi}{4}$.

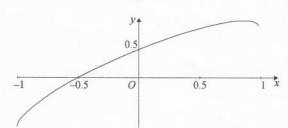
(4)

(c) Find a cartesian equation of the curve in the form y = f(x). State the domain on which the curve is defined.

(4)

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9011191	BIR	11811	62115	HESS	HHI	110101	IBII	20101		ш
8611181		11811	88118		111118	118181	IMII	88161	HILL	118





The curve shown in Figure 2 has parametric equations

$$x = \sin t$$
, $y = \sin (t + \frac{\pi}{6})$, $-\frac{\pi}{2} < t < \frac{\pi}{2}$.

(a) Find an equation of the tangent to the curve at the point where $t = \frac{\pi}{6}$.

(6)

(b) Show that a cartesian equation of the curve is

$$y = \frac{\sqrt{3}}{2}x + \frac{1}{2}\sqrt{(1-x^2)}, \quad -1 < x < 1.$$

(3)

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5

A curve has parametric equations	
$x = \tan^2 t, \qquad y = \sin t, \qquad 0 < t < \frac{\pi}{2}.$	
(a) Find an expression for $\frac{dy}{dx}$ in terms of t. You need not simplify you	r answer.
(b) Find an equation of the tangent to the curve at the point where $t =$	$\frac{\pi}{4}$.
Give your answer in the form $y = ax + b$, where a and b ar determined.	e constants to be
	(5)
(c) Find a cartesian equation of the curve in the form $y^2 = f(x)$.	(4)

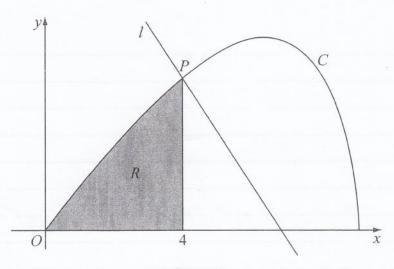


Figure 3

Figure 3 shows the curve C with parametric equations

$$x = 8\cos t$$
, $y = 4\sin 2t$, $0 \le t \le \frac{\pi}{2}$.

The point P lies on C and has coordinates $(4, 2\sqrt{3})$.

(a) Find the value of t at the point P.

(2)

The line l is a normal to C at P.

(b) Show that an equation for l is $y = -x\sqrt{3} + 6\sqrt{3}$.

(6)

The finite region R is enclosed by the curve C, the x-axis and the line x = 4, as shown shaded in Figure 3.

(c) Show that the area of R is given by the integral $\int_{\frac{\pi}{3}}^{\frac{\pi}{2}} 64 \sin^2 t \cos t \, dt.$ (4)

(d) Use this integral to find the area of R, giving your answer in the form $a + b\sqrt{3}$, where a and b are constants to be determined.

(4)

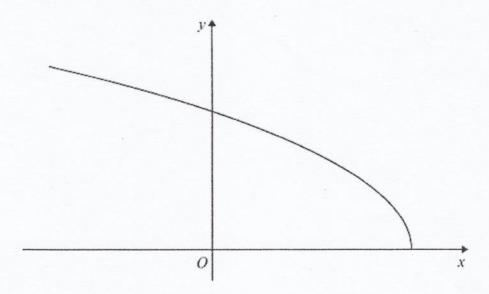


Figure 2

Figure 2 shows a sketch of the curve with parametric equations

$$x = 2\cos 2t, \quad y = 6\sin t, \quad 0 \le t \le \frac{\pi}{2}.$$

(a) Find the gradient of the curve at the point where $t = \frac{\pi}{3}$.

(4)

(b) Find a cartesian equation of the curve in the form

$$y = f(x), -k \le x \le k,$$

stating the value of the constant k.

(4)

(c) Write down the range of f(x).

(2)

4. A curve C has parametric equations

$$x = \sin^2 t$$
, $y = 2 \tan t$, $0 \le t < \frac{\pi}{2}$.

Time

(a) Find $\frac{dy}{dx}$ in terms of t.

(4)

The tangent to C at the point where $t = \frac{\pi}{3}$ cuts the x-axis at the point P.

(b) Find the x-coordinate of P.

7.

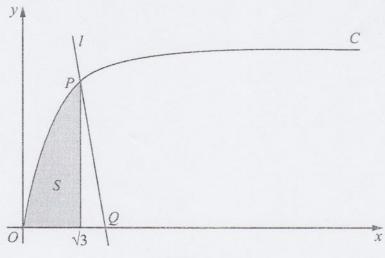


Figure 3

Figure 3 shows part of the curve C with parametric equations

$$x = \tan \theta$$
, $y = \sin \theta$, $0 \le \theta < \frac{\pi}{2}$

The point *P* lies on *C* and has coordinates $\left(\sqrt{3}, \frac{1}{2}\sqrt{3}\right)$.

(a) Find the value of θ at the point P.

(2)

The line l is a normal to C at P. The normal cuts the x-axis at the point Q.

(b) Show that Q has coordinates $(k\sqrt{3}, 0)$, giving the value of the constant k.

(6)

The finite shaded region S shown in Figure 3 is bounded by the curve C, the line $x = \sqrt{3}$ and the x-axis. This shaded region is rotated through 2π radians about the x-axis to form a solid of revolution.

(c) Find the volume of the solid of revolution, giving your answer in the form $p \pi \sqrt{3 + q \pi^2}$, where p and q are constants.

(7)



6.

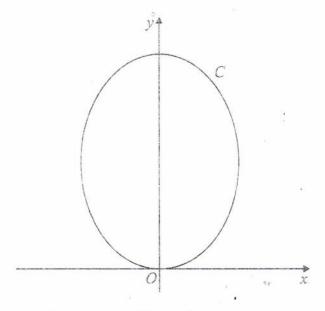


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = (\sqrt{3})\sin 2t$$
, $y = 4\cos^2 t$, $0 \le t \le \pi$

(a) Show that $\frac{dy}{dx} = k(\sqrt{3})\tan 2t$, where k is a constant to be determined.

(5)

(b) Find an equation of the tangent to C at the point where $t = \frac{\pi}{3}$. Give your answer in the form y = ax + b, where a and b are constants.

(4)

(c) Find a cartesian equation of C.

(3)

5.

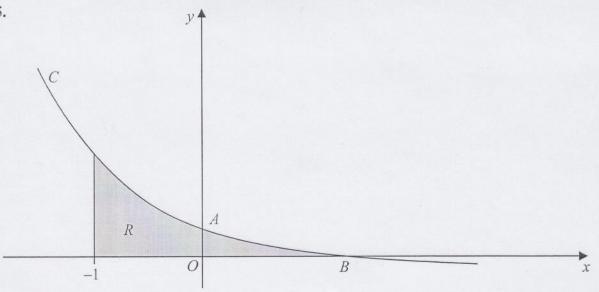


Figure 2

Figure 2 shows a sketch of part of the curve C with parametric equations

$$x = 1 - \frac{1}{2}t$$
, $y = 2^t - 1$

The curve crosses the y-axis at the point A and crosses the x-axis at the point B.

(a) Show that A has coordinates (0, 3).

(2)

(b) Find the x coordinate of the point B.

(2)

(c) Find an equation of the normal to C at the point A.

(5)

The region R, as shown shaded in Figure 2, is bounded by the curve C, the line x = -1 and the x-axis.

(d) Use integration to find the exact area of R.

(6)

12

4. A curve C has parametric equations

$$x = 2\sin t$$
, $y = 1 - \cos 2t$, $-\frac{\pi}{2} \leqslant t \leqslant \frac{\pi}{2}$

(a) Find $\frac{dy}{dx}$ at the point where $t = \frac{\pi}{6}$

(4)

(b) Find a cartesian equation for C in the form

$$y = f(x), -k \le x \le k,$$

stating the value of the constant k.

(3)

(c) Write down the range of f(x).

(2)

4	