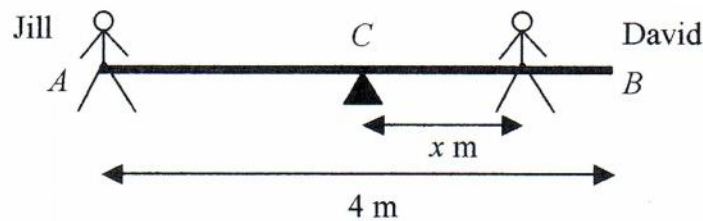


3.

Figure 1



A seesaw in a playground consists of a beam AB of length 4 m which is supported by a smooth pivot at its centre C . Jill has mass 25 kg and sits on the end A . David has mass 40 kg and sits at a distance x metres from C , as shown in Figure 1. The beam is initially modelled as a uniform rod. Using this model,

(a) find the value of x for which the seesaw can rest in equilibrium in a horizontal position. (3)

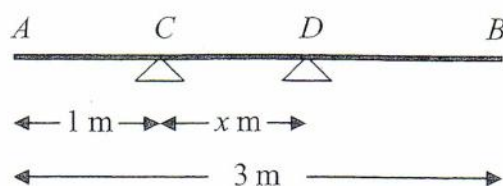
(b) State what is implied by the modelling assumption that the beam is uniform. (1)

David realises that the beam is not uniform as he finds he must sit at a distance 1.4 m from C for the seesaw to rest horizontally in equilibrium. The beam is now modelled as a non-uniform rod of mass 15 kg. Using this model,

(c) find the distance of the centre of mass of the beam from C . (4)

2.

Figure 2



A uniform plank AB has weight 120 N and length 3 m . The plank rests horizontally in equilibrium on two smooth supports C and D , where $AC = 1\text{ m}$ and $CD = x\text{ m}$, as shown in Figure 2. The reaction of the support on the plank at D has magnitude 80 N . Modelling the plank as a rod,

- (a) show that $x = 0.75$ (3)

A rock is now placed at B and the plank is on the point of tilting about D . Modelling the rock as a particle, find

- (b) the weight of the rock, (4)
- (c) the magnitude of the reaction of the support on the plank at D . (2)
- (d) State how you have used the model of the rock as a particle. (1)



A horizontal line segment is shown with endpoints labeled A and B . A point C is located on the segment between A and B . Vertical lines are drawn at A and C . Below the segment, a double-headed arrow indicates the distance from A to C is 5 m . Another double-headed arrow indicates the distance from C to B is 1 m .

A beam AB has mass 12 kg and length 5 m . It is held in equilibrium in a horizontal position by two vertical ropes attached to the beam. One rope is attached to A , the other to the point C on the beam, where $BC = 1\text{ m}$, as shown in Figure 2. The beam is modelled as a uniform rod, and the ropes as light strings.

(5)

(3)

(3)

This image shows a single sheet of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page. There is no handwriting or other markings on the paper.

Diagram of a beam of length 2.4 m. The beam is supported by two vertical supports. The left support is at point Q, and the right support is at point R. The distance from the left end P to Q is 0.4 m, and the distance from R to the right end S is 0.4 m.

A bench consists of a plank which is resting in a horizontal position on two thin vertical legs. The plank is modelled as a uniform rod PS of length 2.4 m and mass 20 kg. The legs at Q and R are 0.4 m from each end of the plank, as shown in Figure 1.

(a) the magnitude of the normal reaction between the plank and the leg at Q and the magnitude of the normal reaction between the plank and the leg at R .

Beatrice stays sitting at P but Arthur now moves and sits on the plank at the point X . Given that the plank remains horizontal and in equilibrium, and that the magnitude of the normal reaction between the plank and the leg at Q is now twice the magnitude of the normal reaction between the plank and the leg at R ,

(6)

The diagram shows a horizontal beam ABC. Point A is on the left, point C is in the middle, and point B is on the right. A vertical line segment is drawn at point C, representing a reaction. A double-headed arrow below the beam indicates the distance from A to C is 1.8 m. Another double-headed arrow below the beam indicates the distance from C to B is 3 m. The total length of the beam AB is 4.8 m.

A pole AB has length 3 m and weight W newtons. The pole is held in a horizontal position in equilibrium by two vertical ropes attached to the pole at the points A and C where $AC = 1.8$ m, as shown in Figure 2. A load of weight 20 N is attached to the rod at B . The pole is modelled as a uniform rod, the ropes as light inextensible strings and the load as a particle.

- (b) Find, in terms of W , the tension in the rope attached to the pole at A . (3)

Given that the tension in the rope attached to the pole at C is eight times the tension in the rope attached to the pole at A ,

- (c) find the value of W . (3)

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A horizontal beam of length 6 m is shown, with points A, C, and B marked. A roller support is located at point C, which is 1 m from point A. The total length of the beam is indicated as 6 m.

A uniform beam AB has mass 20 kg and length 6 m . The beam rests in equilibrium in a horizontal position on two smooth supports. One support is at C , where $AC = 1\text{ m}$, and the other is at the end B , as shown in Figure 1. The beam is modelled as a rod.

- A boy of mass 30 kg stands on the beam at the point D . The beam remains in equilibrium. The magnitudes of the reactions on the beam at B and at C are now equal. The boy is modelled as a particle.

- (b) Find the distance AD . (5)

Diagram of a beam AB of length $5d$. The beam is supported by two triangular supports at points C and D . The distance from A to C is d , and the distance from D to B is d . The center of gravity G is marked on the beam between C and D . The total length of the beam is indicated as $5d$ at the bottom.

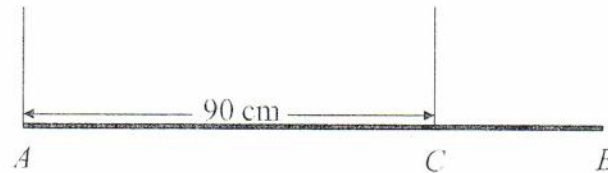
A non-uniform rod AB , of mass m and length $5d$, rests horizontally in equilibrium on two supports at C and D , where $AC = DB = d$, as shown in Figure 1. The centre of mass of the rod is at the point G . A particle of mass $\frac{5}{2}m$ is placed on the rod at B and the rod is on the point of tipping about D .

- The particle is moved from B to the mid-point of the rod and the rod remains in equilibrium.

- (b) Find the magnitude of the normal reaction between the support at D and the rod. (5)

5.

Figure 3



A steel girder AB has weight 210 N . It is held in equilibrium in a horizontal position by two vertical cables. One cable is attached to the end A . The other cable is attached to the point C on the girder, where $AC = 90\text{ cm}$, as shown in Figure 3. The girder is modelled as a uniform rod, and the cables as light inextensible strings.

Given that the tension in the cable at C is twice the tension in the cable at A , find

- (a) the tension in the cable at A ,

(2)

- (b) show that $AB = 120\text{ cm}$.

(4)

A small load of weight W newtons is attached to the girder at B . The load is modelled as a particle. The girder remains in equilibrium in a horizontal position. The tension in the cable at C is now three times the tension in the cable at A .

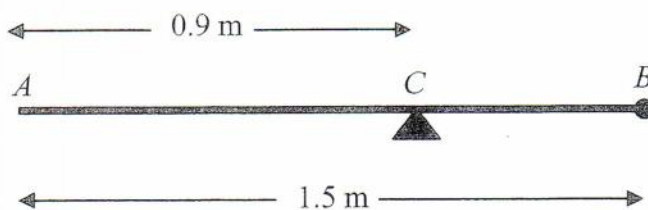
- (c) Find the value of W .

(7)



3.

Figure 2



A uniform rod AB has length 1.5 m and mass 8 kg. A particle of mass m kg is attached to the rod at B . The rod is supported at the point C , where $AC = 0.9$ m, and the system is in equilibrium with AB horizontal, as shown in Figure 2.

(a) Show that $m = 2$.

(4)

A particle of mass 5 kg is now attached to the rod at A and the support is moved from C to a point D of the rod. The system, including both particles, is again in equilibrium with AB horizontal.

(b) Find the distance AD .

(5)



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7.

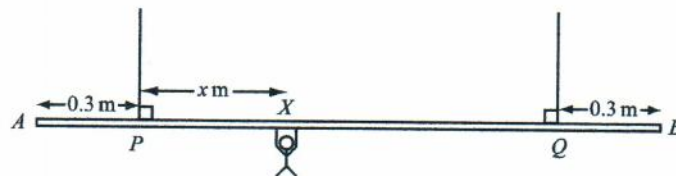


Figure 2

A beam AB is supported by two vertical ropes, which are attached to the beam at points P and Q , where $AP = 0.3$ m and $BQ = 0.3$ m. The beam is modelled as a uniform rod, of length 2 m and mass 20 kg. The ropes are modelled as light inextensible strings. A gymnast of mass 50 kg hangs on the beam between P and Q . The gymnast is modelled as a particle attached to the beam at the point X , where $PX = x$ m, $0 < x < 1.4$ as shown in Figure 2. The beam rests in equilibrium in a horizontal position.

- Show that the tension in the rope attached to the beam at P is $(588 - 350x)$ N. (3)
 - Find, in terms of x , the tension in the rope attached to the beam at Q . (3)
 - Hence find, justifying your answer carefully, the range of values of the tension which could occur in each rope. (3)
- Given that the tension in the rope attached at Q is three times the tension in the rope attached at P ,
- find the value of x . (3)



Diagram of a horizontal beam ABE. A vertical wall is at point A, and a roller support is at point C. The distance from A to C is 0.8 m, and the distance from C to E is 2.4 m.

A plank AB has mass 12 kg and length 2.4 m . A load of mass 8 kg is attached to the plank at the point C , where $AC = 0.8\text{ m}$. The loaded plank is held in equilibrium, with AB horizontal, by two vertical ropes, one attached at A and the other attached at B , as shown in Figure 2. The plank is modelled as a uniform rod, the load as a particle and the ropes as light inextensible strings.

- The plank is now modelled as a non-uniform rod. With the new model, the tension in the rope attached at A is 10 N greater than the tension in the rope attached at B .

4. A beam AB has length 6 m and weight 200 N. The beam rests in a horizontal position on two supports at the points C and D , where $AC = 1$ m and $DB = 1$ m. Two children, Sophie and Tom, each of weight 500 N, stand on the beam with Sophie standing twice as far from the end B as Tom. The beam remains horizontal and in equilibrium and the magnitude of the reaction at D is three times the magnitude of the reaction at C . By modelling the beam as a uniform rod and the two children as particles, find how far Tom is standing from the end B .

(7)



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2. A steel girder AB , of mass 200 kg and length 12 m, rests horizontally in equilibrium on two smooth supports at C and at D , where $AC = 2$ m and $DB = 2$ m. A man of mass 80 kg stands on the girder at the point P , where $AP = 4$ m, as shown in Figure 1.

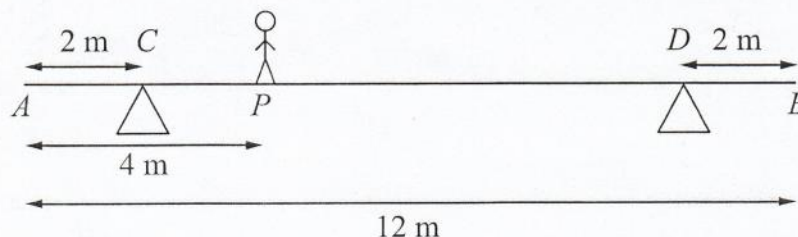


Figure 1

The man is modelled as a particle and the girder is modelled as a uniform rod.

- (a) Find the magnitude of the reaction on the girder at the support at C .

(3)

The support at D is now moved to the point X on the girder, where $XB = x$ metres. The man remains on the girder at P , as shown in Figure 2.

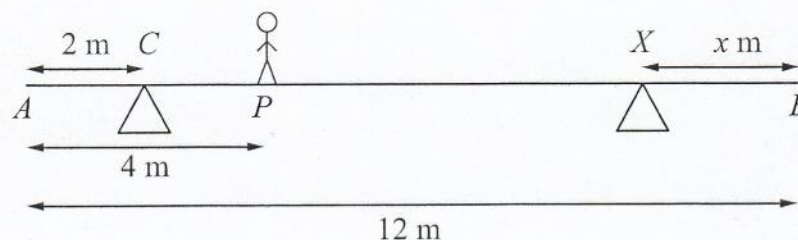


Figure 2

Given that the magnitudes of the reactions at the two supports are now equal and that the girder again rests horizontally in equilibrium, find

- (b) the magnitude of the reaction at the support at X ,

(2)

- (c) the value of x .

(4)



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- (a) (i) Find the mass of the beam.

- (8)

(b) find AX .

(6)

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